

Optimal dynamic control of the forest resource with changing energy demand functions and valuation of CO2 storage

Presentation at the Conference:

***The European Forest-based Sector:
Bio-Responses to Address New Climate and Energy Challenges?
Nancy, France, November 6-8, 2008***

Peter Lohmander

***Professor of Forest Management and Economic Optimization
SLU, Swedish University of Agricultural Sciences
Umea, Sweden***

<http://www.Lohmander.com>

Structure of the presentation:

- #1. Introduction to rational use of the forest when we consider CO2 and energy production***
- #2. Optimal dynamic control of the forest resource with changing energy demand functions and valuation of CO2 storage***
- #3. Optimal CCS, Carbon Capture and Storage, Under Risk***
- #4. Conclusions***

***#1. Introduction to rational use of
the forest when we consider CO₂
and energy production***

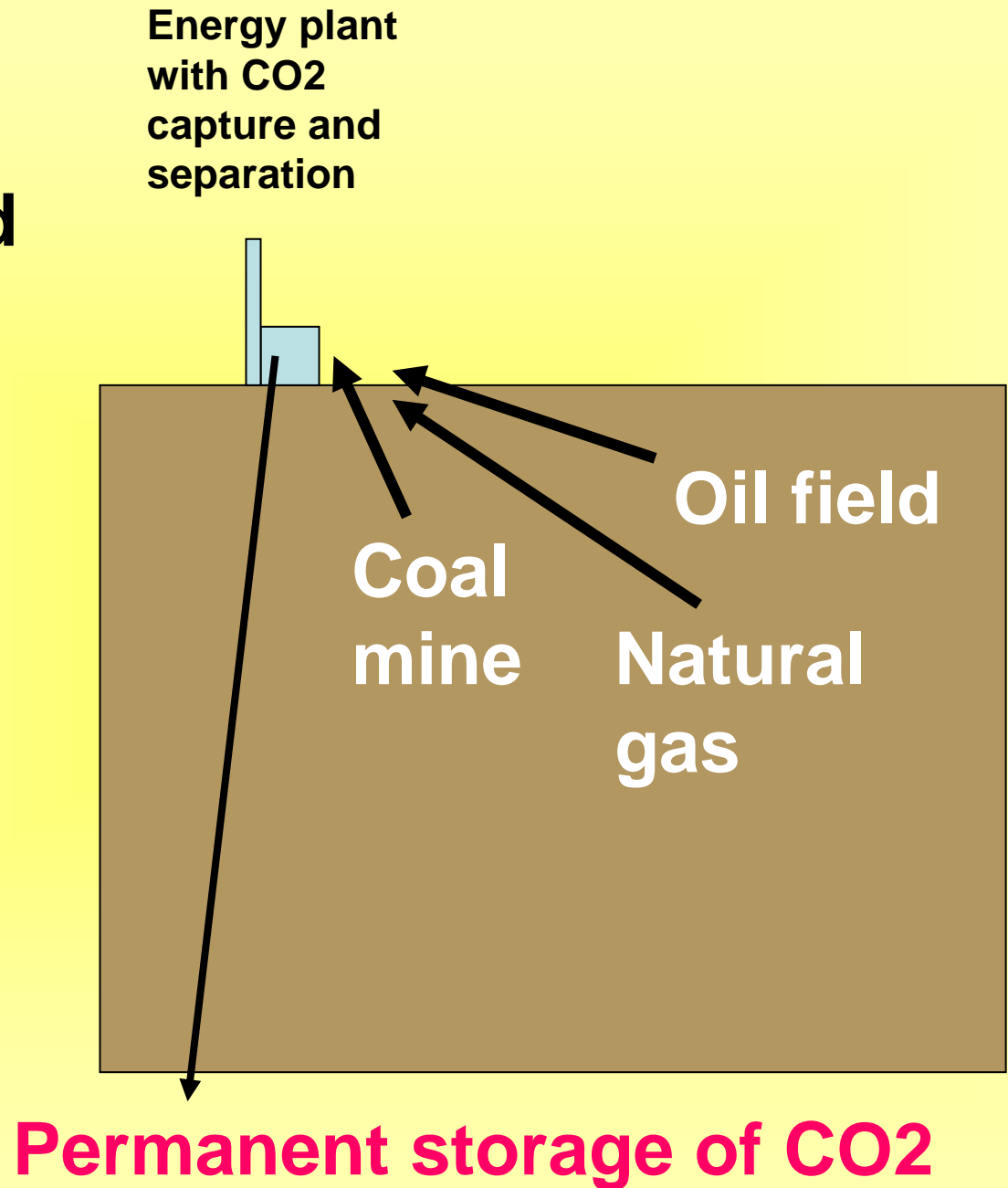
The role of the forest?

- The best way to reduce the CO₂ in the atmosphere may be to ***increase harvesting of the presently existing forests (!)***, to produce energy with CCS and to increase forest production in the new forest generations.
- ***We capture and store more CO₂!***

The role of the forest?

- The best way to reduce the CO₂ in the atmosphere may be to ***increase harvesting of the presently existing forests (!)***, to produce energy with CCS and to increase forest production in the new forest generations.
- ***We capture and store more CO₂!***

**CCS,
Carbon
Capture and
Storage,
has already
become
the main
future
emission
reduction
method of
the fossile
fuel energy
industry**



BBC World News 2008-10-17:

- ***The British government declares that the CO2 emissions will be reduced by 80% by 2050!***
- ***CCS is the method to be used in combination with fossile fuels such as coal.***

Reference to CCS in the energy industry and EU policy

2nd Annual EMISSIONS REDUCTION FORUM: - Establishing Effective CO₂, NO_x, SO_x Mitigation Strategies for the Power Industry, CD, Marcus Evans Ltd, Madrid, Spain, 29th & 30th September 2008

The CD (above) includes presentations where several dominating European energy companies show how they develop and use CCS and where the European Commission gives the general European emission and energy policy perspective.

Conference programme:

<http://www.lohmander.com/Madrid08/MadridProg08.pdf>

Lohmander, P., Guidelines for Economically Rational and Coordinated Dynamic Development of the Forest and Bio Energy Sectors with CO2 constraints, Proceedings from the 16th European Biomass Conference and Exhibition, Valencia, Spain, 02-06 June, 2008 (In the version in the link, below, an earlier misprint has been corrected.)
<http://www.Lohmander.com/Valencia2008.pdf>

Lohmander, P., Economically Optimal Joint Strategy for Sustainable Bioenergy and Forest Sectors with CO2 Constraints, European Biomass Forum, Exploring Future Markets, Financing and Technology for Power Generation, CD, Marcus Evans Ltd, Amsterdam, 16th-17th June, 2008
<http://www.Lohmander.com/Amsterdam2008.ppt>

Lohmander, P., Tools for optimal coordination of CCS, power industry capacity expansion and bio energy raw material production and harvesting, 2nd Annual EMISSIONS REDUCTION FORUM: - Establishing Effective CO₂, NO_x, SO_x Mitigation Strategies for the Power Industry, CD, Marcus Evans Ltd, Madrid, Spain, 29th & 30th September 2008

http://www.lohmander.com/Madrid08/Madrid_2008_Lohmander.ppt

Lohmander, P., Optimal CCS, Carbon Capture and Storage, Under Risk, International Seminars in Life Sciences, UPV, Universidad Politécnicna de Valencia, Thursday 2008-10-16

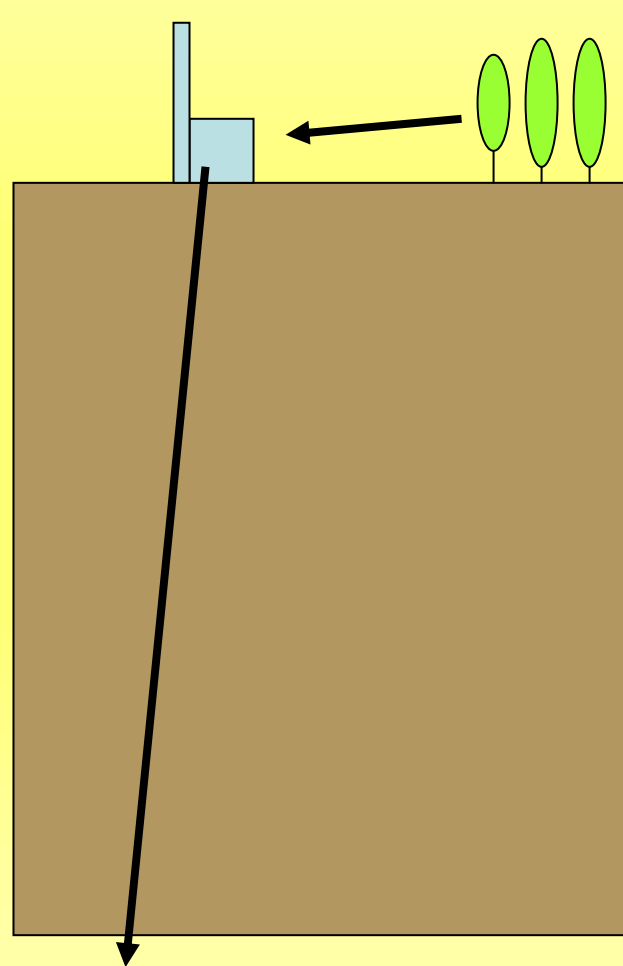
<http://www.Lohmander.com/OptCCS/OptCCS.ppt>

**How to
reduce the
CO2 level in
the
atmosphere,**

***not only to
decrease the
emission of
CO2***

Energy plant
with CO2
capture and
separation

CO2

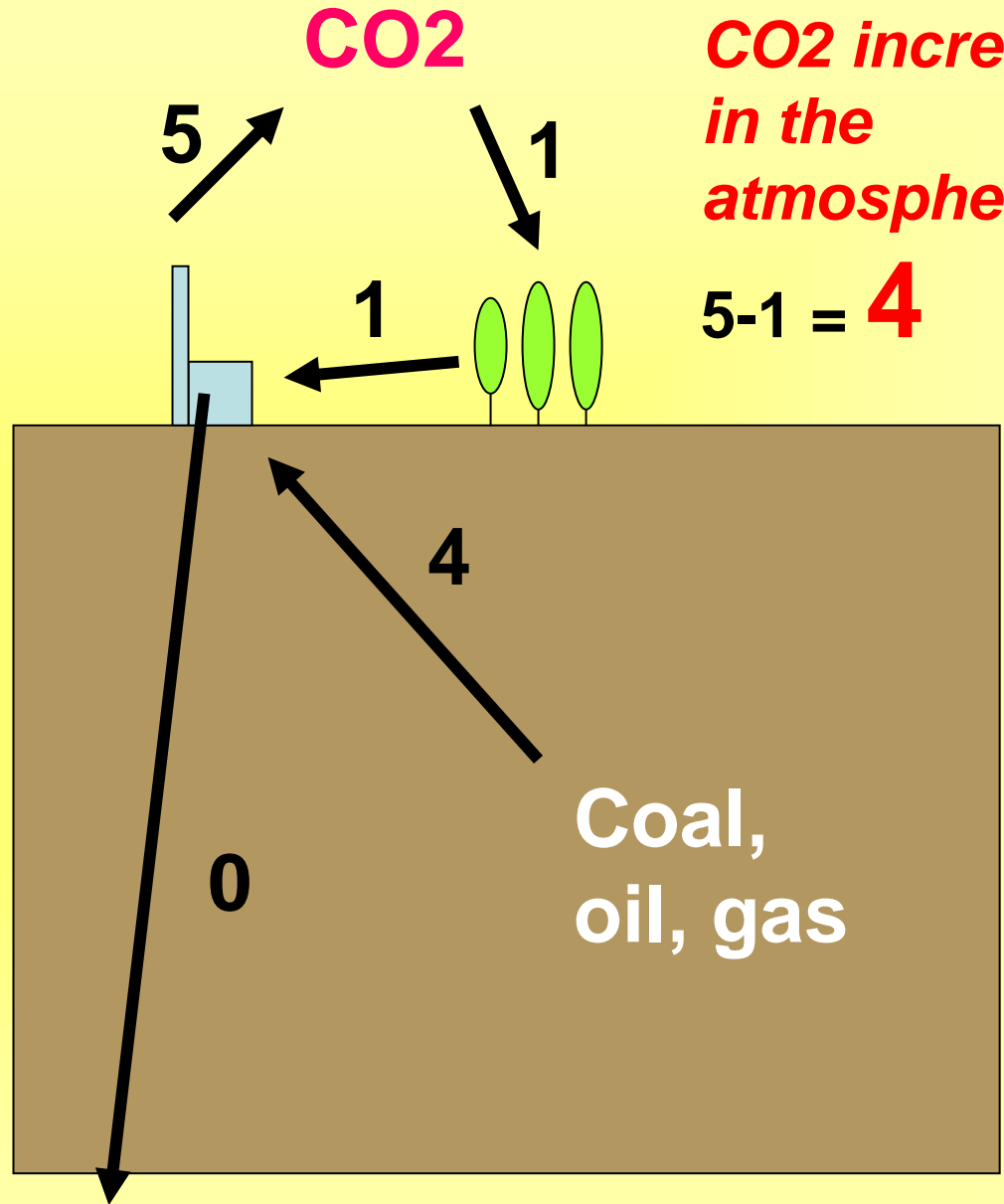


Permanent storage of CO2

The role of the forest in the CO₂ and energy system

- *The following six pictures show that it is necessary to intensify the use of the forest for energy production in combination with CCS in order to reduce the CO₂ in atmosphere!*
- All figures and graphs have been simplified as much as possible, keeping the big picture correct, in order to make the main point obvious.
- In all cases, we keep the total energy production constant.

The present situation.



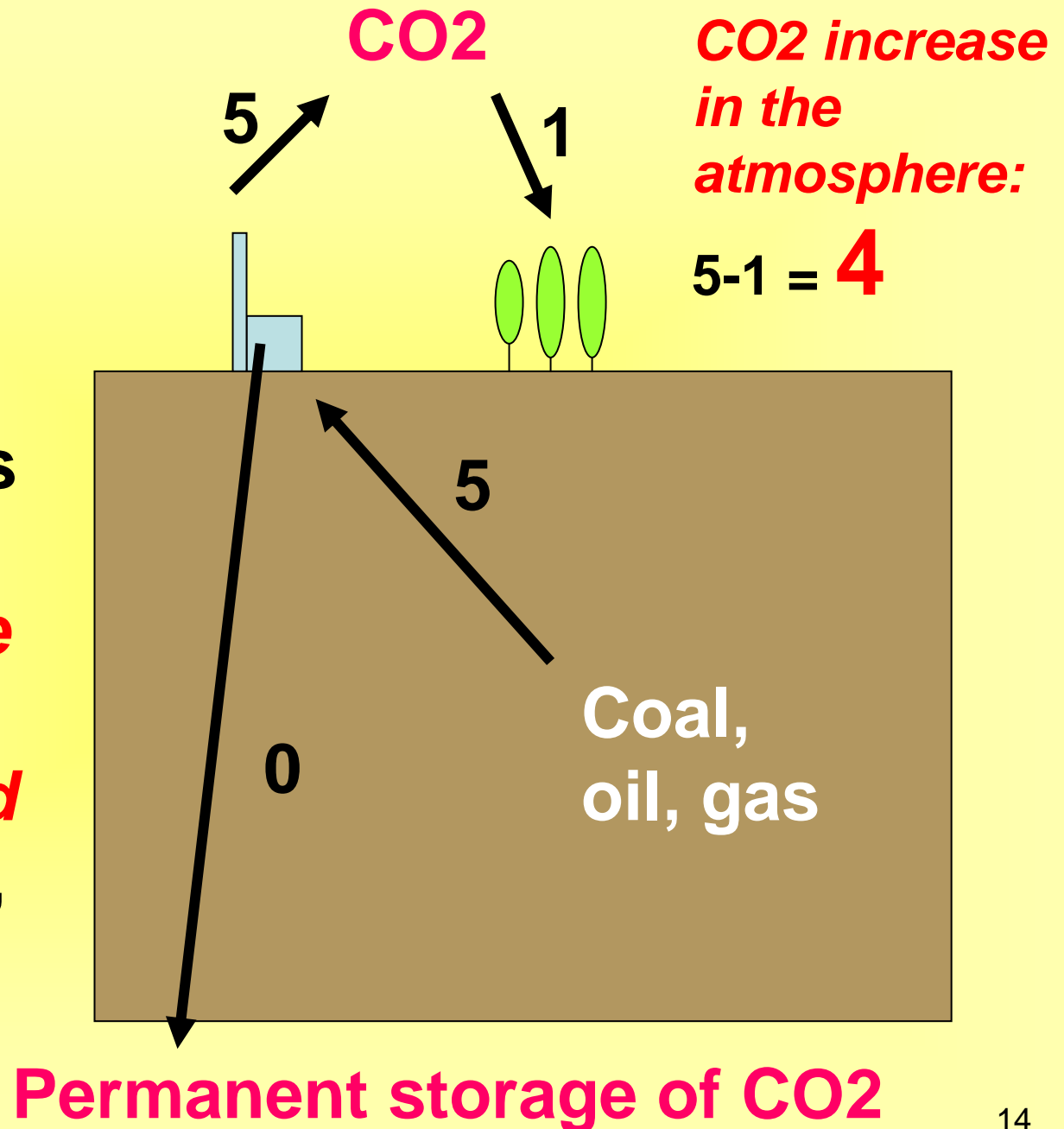
CO2

CO2 increase in the atmosphere:

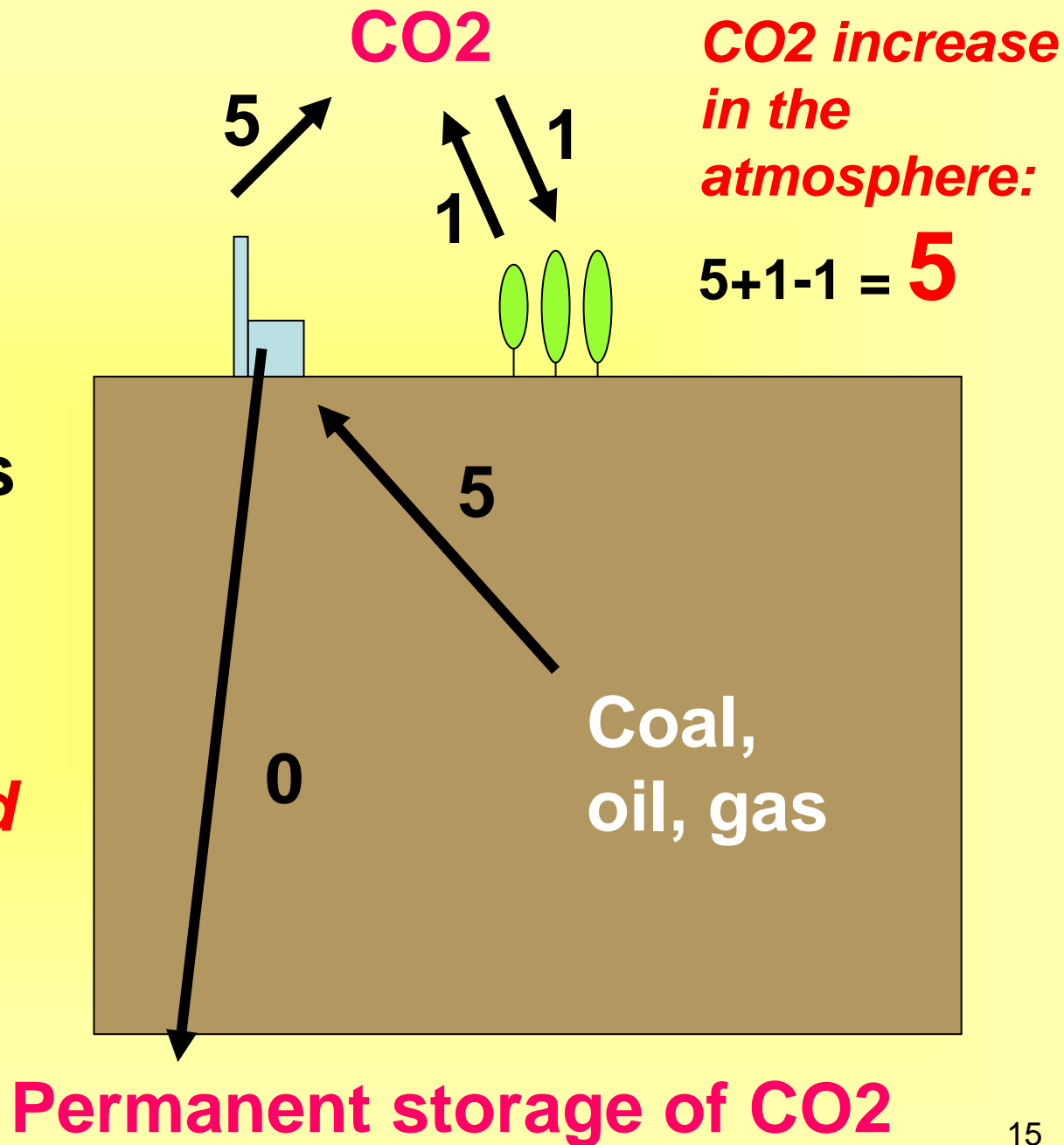
$5 - 1 = 4$

Permanent storage of CO2

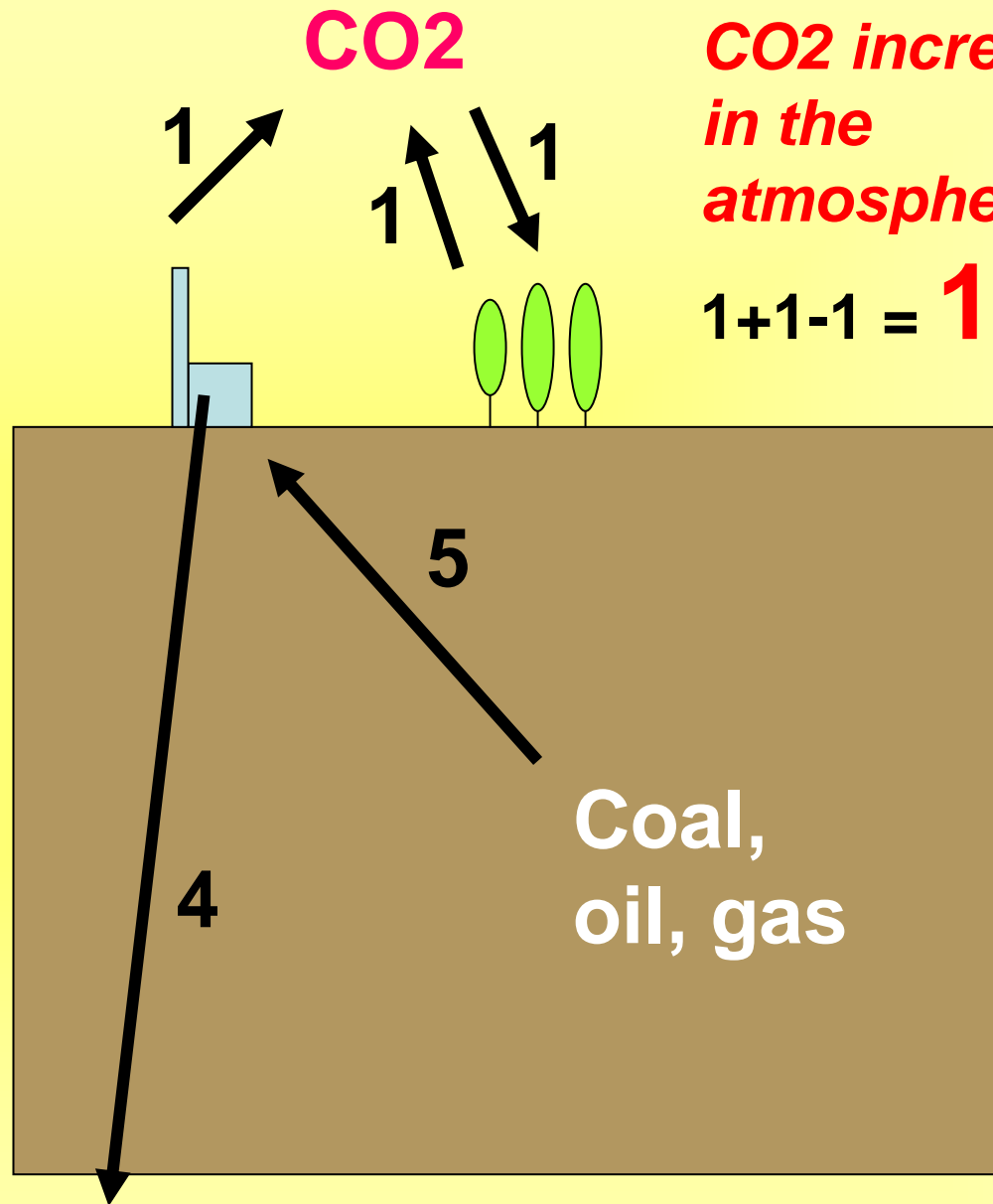
If we do not use the forest for energy production but use it as a carbon sink. *Before the forest has reached equilibrium, this happens:*



If we do not use the forest for energy production but use it as a carbon sink. *When the forest has reached equilibrium, this happens:*



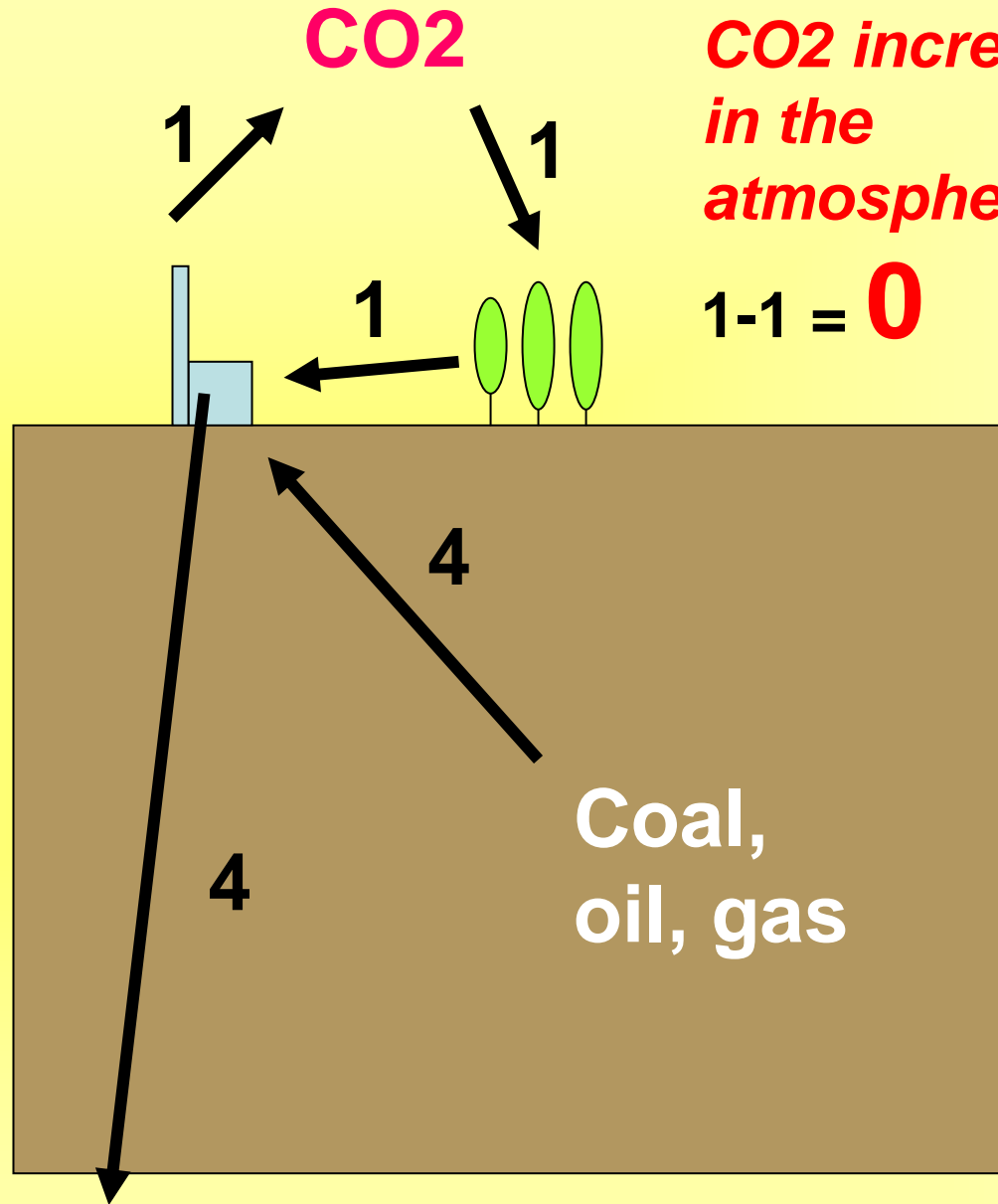
If we use
CCS with
80%
efficiency
and let the
forest grow
until it
reaches
equilibrium.



*CO2 increase
in the
atmosphere:*
 $1+1-1 = 1$

Permanent storage of CO2

If we use CCS with 80% efficiency and use the forest with "traditional" low intensity harvesting and silviculture.

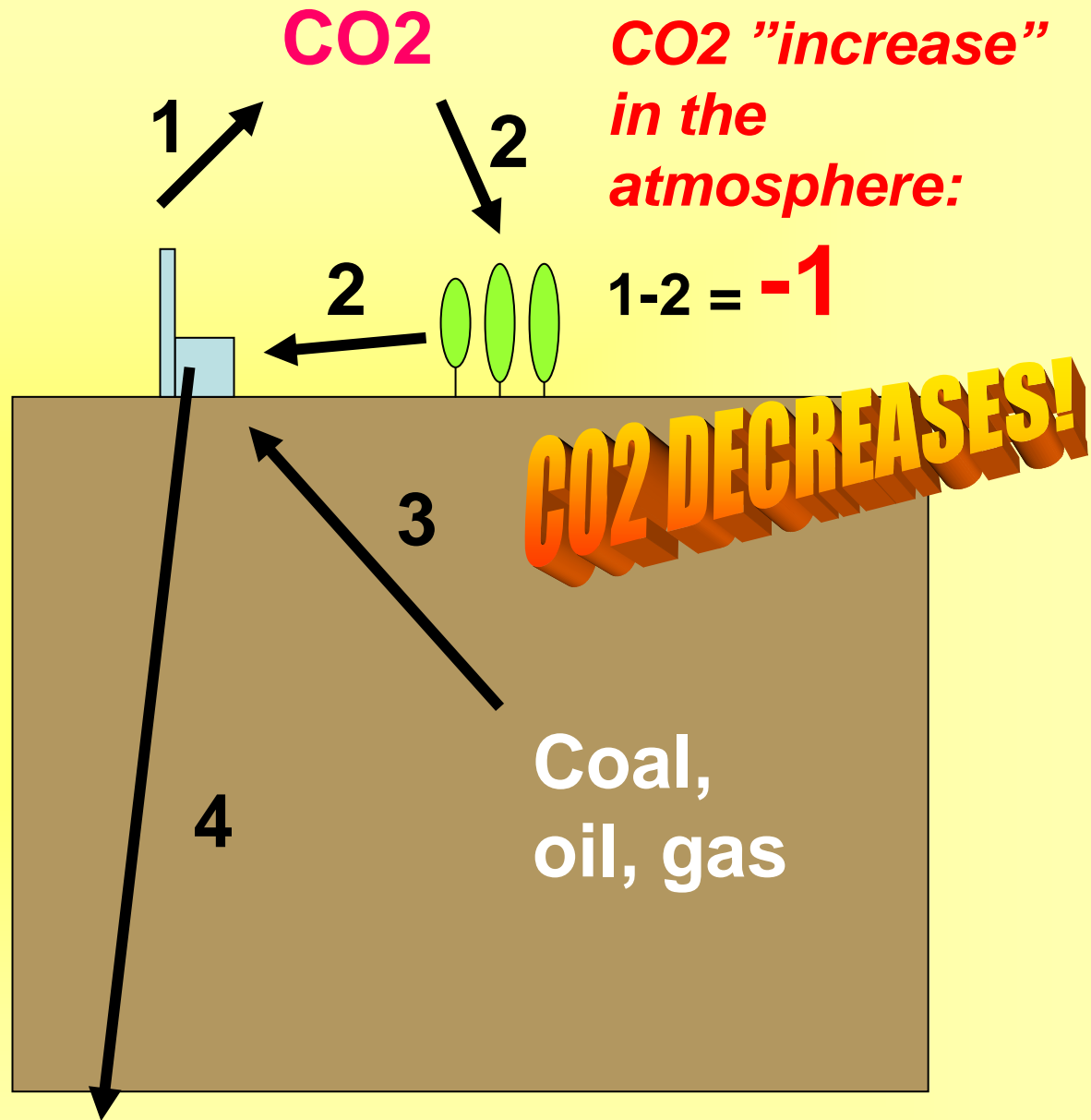


CO2

CO2 increase in the atmosphere:
 $1 - 1 = 0$

Permanent storage of CO2

If we use CCS with 80% efficiency and use the forest with increased harvesting and high intensity silviculture.



Permanent storage of CO₂

General conclusions:

- The best way to reduce the CO₂ in the atmosphere may be to ***increase harvesting of the presently existing forests (!)***, to produce energy with CCS and to increase forest production in the new forest generations.
- ***We capture and store more CO₂!***

#2. Optimal dynamic control of the forest resource with changing energy demand functions and valuation of CO₂ storage

The optimal control derivations and the software are found here:

Lohmander, P., Optimal resource control model & General continuous time optimal control model of a forest resource, comparative dynamics and CO2 consideration effects, Seminar at SLU, Umea, Sweden, 2008-09-18

<http://www.lohmander.com/CM/CMLohmander.ppt>

Software:

<http://www.lohmander.com/CM/CM.htm>

Economic valuation of CO2 storage in the natural resource

Economic Valuation of the Production of Energy and Other Industrial Products

$$\max \left\{ J = \int_{t_1}^{t_2} e^{-rt} \left((f_1 + f_2 t) x + (k_1 + k_2 t) u + k_3 u^2 \right) dt \right\}$$


The Total Economic Result (Present Value)

The Stock Level

The "Control" Level

•

$$\dot{x} = f(x, u, t) \quad ; \quad x(t_1) = x_1, \quad x(t_2) = x_2$$



**The change of
the stock level
during a marginal
time interval**

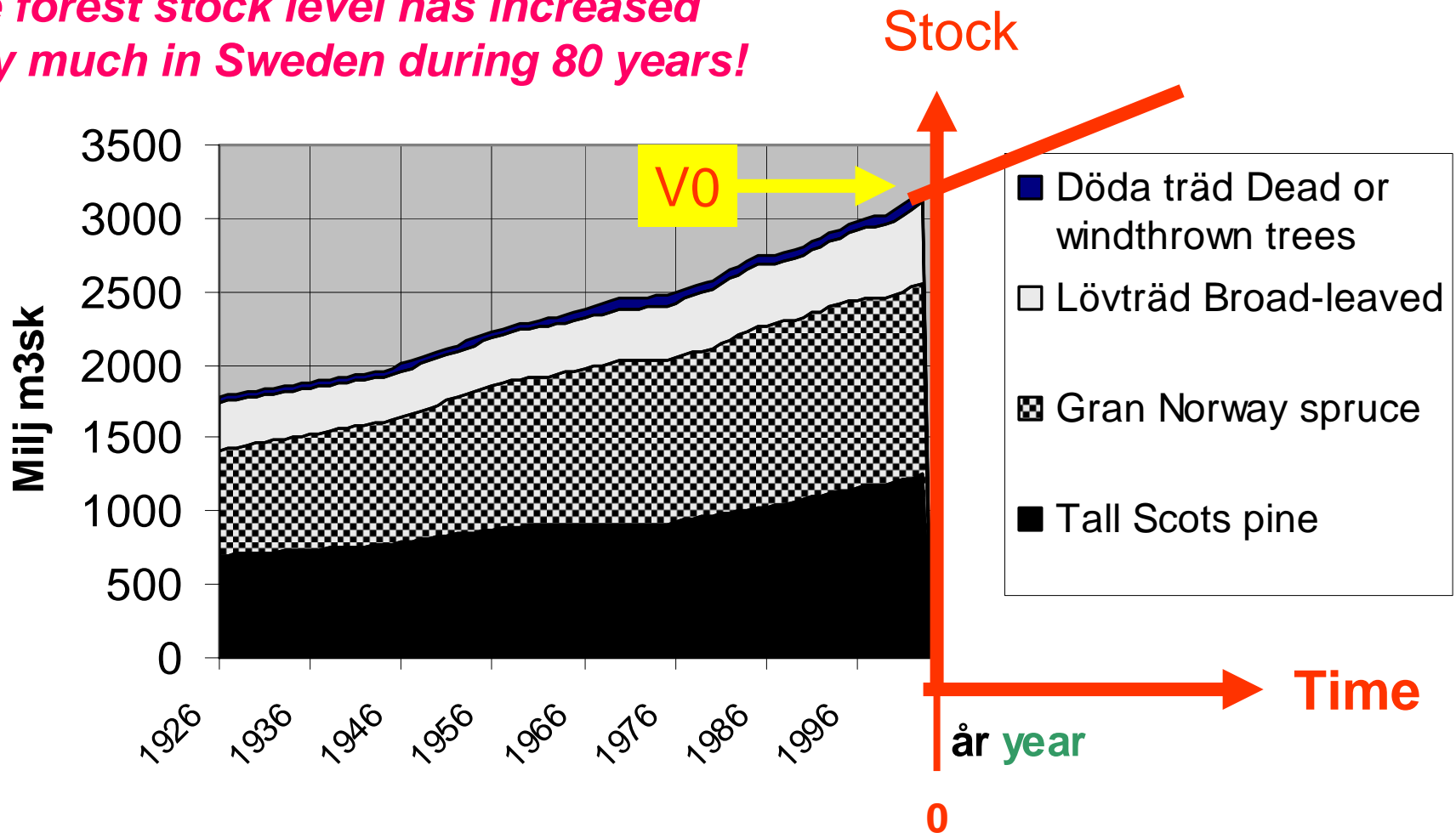


Initial stock level



Terminal stock level

The forest stock level has increased very much in Sweden during 80 years!

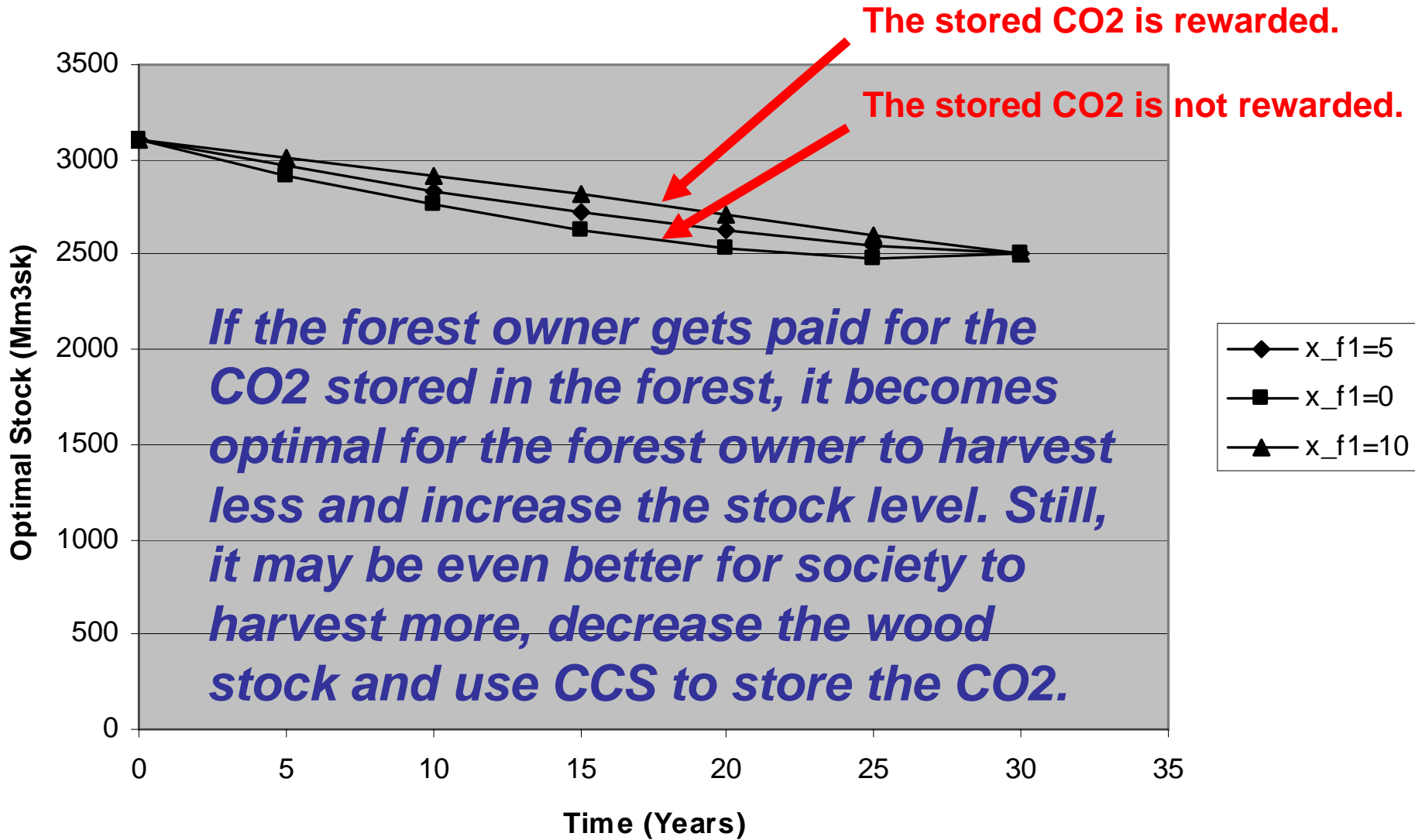


1 Exkl. fjäll, fridlyst mark, militära impediment, bebyggd mark samt söt- och saltvatten.

Excl. high mountains, restricted military areas, urban land and water surfaces.

Milj. M3sk Millions cubic metre standing volume (stem volume over bark from stump to tio)

Optimal Stock Path



#3. Optimal CCS, Carbon Capture and Storage, Under Risk

The stochastic optimal control derivations of CCS are found here:

- **Lohmander, P., Optimal CCS, Carbon Capture and Storage, Under Risk, *International Seminars in Life Sciences, Universidad Politécnica de Valencia, Thursday 2008-10-16***
- **<http://www.Lohmander.com/OptCCS/OptCCS.ppt>**

Optimal CCS, Carbon Capture and Storage, Under Risk

The objective function is the total present value of CO2 storage minus CCS costs.

$$\int_0^{\infty} e^{-rt} \left(k_1 u + k_2 u^2 + f_1 x + f_2 x^2 \right) dt$$

Discounting factor

$u =$
control =
CCS
level

$x =$ The total
storage level
of CO2

The controlled storage

A stochastic differential equation:

$$dx = (u - Lx - S) dt + \sigma x dz$$

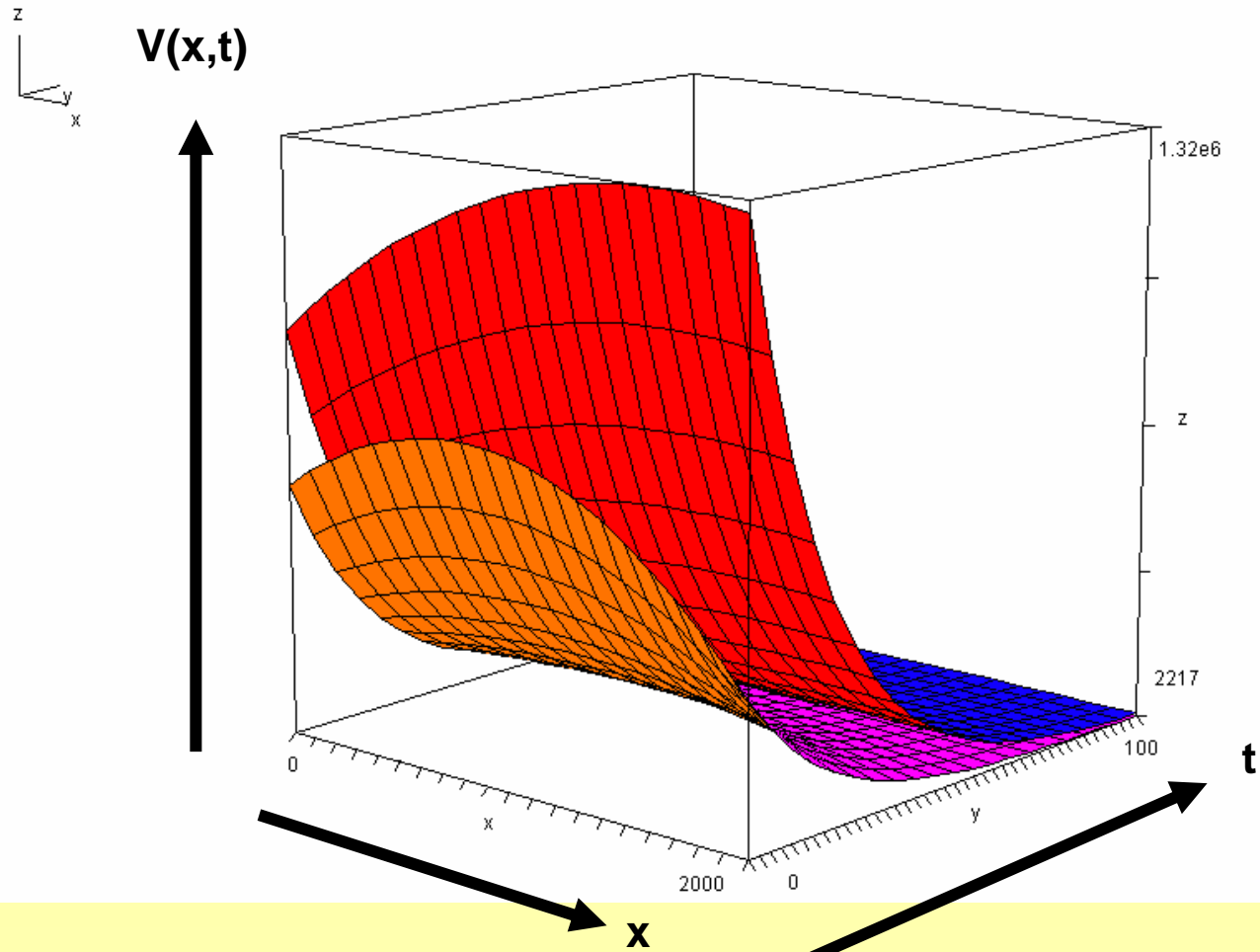
Change of the
CO2 storage level.

Control =
CCS level.

Expected CO2 leakage.

The CO2 storage level is to some extent affected by stochastic leakage and other stochastic events.
Z = standard Wiener process.

The optimal CCS objective function for different risk levels. The details are found in the reference.



#4. Conclusions

Optimal Forest management conclusions:

- If the forest owner gets paid for the CO₂ stored in the forest, it becomes optimal for the forest owner to harvest less and increase the stock level. Still, it may be even better for society to harvest more, decrease the present wood stock and use CCS to store the CO₂.
- The best way to reduce the CO₂ in the atmosphere may be to *increase harvesting of the presently existing forests (!)*, to produce energy with CCS and to increase forest production in the new forest generations.

Optimal CCS Conclusions:

- **A mathematical approach to optimal CCS control has been developed that can handle risk.**
- **Possible leakage is an important issue that has to be carefully investigated in the future.**
- **It is important that the future management decisions are based on a decision model consistent with the structure of this model and that the parameter values are carefully estimated before practical management decisions are calculated.**

Future discussions:

Peter Lohmander is organizing the conference stream “Optimal Forest Management with Increasing Bioenergy Demand” within The 23rd European Conference on Operational Research (EURO XXIII), July 5-8, 2009, Bonn, Germany.

<http://www.lohmander.com/Bonn2009/Bonn2009.pdf>

Let us continue our discussions and meet there!

Thank you for listening!

Here you may reach me in the future:

Peter Lohmander

**Professor of Forest Management and Economic Optimization,
SLU, Swedish University of Agricultural Sciences, Faculty of Forest Sciences,
Dept. Of Forest Economics, SE-901 83 Umea, Sweden**

<http://www.Lohmander.com>

Peter@Lohmander.com

peter.lohmander@sekon.slu.se

***My warmest "Thanks" to E.ON
Sweden for economic support to the
project "Economic forest production
with consideration of the forest- and
energy- industries"!***

Peter Lohmander

*Professor of Forest Management and Economic Optimization, Swedish University of Agricultural
Sciences*

<http://www.Lohmander.com>

Peter@Lohmander.com